

Term 1 When would you use Substitution to solve Simultaneous Equations?	Definition 1 When one variable can be easily expressed in terms of the other
Term 2 When would you solve 2 simultaneous equations by Combination?	Definition 2 Whenever it's easy to manipulate the equations so that the coefficients for one variable are the SAME or OPPOSITE
Term 3 If you plan to ADD 2 simultaneous equations to solve by combination, what should you do?	Definition 3 Multiply ONE or BOTH of the equations so that the coefficient of a variable in one equation is the OPPOSITE of that variable's coefficient in the other equation

Term 4

If you plan to **SUBTRACT 2** simultaneous equations by combination, what should you do?

Definition 4

Multiply ONE or BOTH of the equations so that the coefficient of a variable in one equation is the SAME of that variable's coefficient in the other equation

Term 5

How would you solve 3 simultaneous equations with 3 variables in each?

Definition 5

Using substitution or combination, or both

Term 6

What's the sum of x, y and z ?:

$$\begin{array}{r} x + y = 8 \\ x + z = 11 \\ y + z = 7 \end{array}$$

Definition 6

$$\begin{array}{r} x + y = 8 \\ x + \quad + z = 11 \\ \quad + y + z = 7 \\ \hline 2x + 2y + 2z = 26 \\ \text{thus, } x + y + z = 13 ! \end{array}$$

<p>Term 7</p> <p>What is the rule for determining whether 2 equations involving 2 variables (say, x and y) will be sufficient to solve for the variables?</p>	<p>Definition 7</p> <p>1) If both equations are LINEAR (i.e. no squared terms and no xy terms) - the equations are SUFFICIENT, <i>UNLESS</i> the two equations are MATHEMATICALLY IDENTICAL</p> <p>2) If there are ANY non-linear terms in either of the equations (i.e. x^3, xy or x/y), there will USUALLY be 2 more different solutions for each of the variables, and the equations will NOT be sufficient.</p>
<p>Term 8</p> <p>When solving 2 equations involving 2 variables, if both equations are LINEAR (i.e. no squared terms and no xy terms)... CAN you solve them? Why/Why not?</p>	<p>Definition 8</p> <p>YES</p> <p>If both equations are LINEAR (i.e. no squared terms and no xy terms) - the equations are SUFFICIENT to solve the question, <i>UNLESS</i> the two equations are MATHEMATICALLY IDENTICAL</p>
<p>Term 9</p> <p>2 equations with 2 variables have a non-linear term in one of the equations. Are they solvable? Why/Why Not?</p>	<p>Definition 9</p> <p>NO</p> <p>If there are ANY non-linear terms in either of the equations (i.e. x^3, xy or x/y), there will USUALLY be 2 more different solutions for each of the variables, and the equations will NOT be sufficient.</p>

Term 10 What should you do when you see a COMBO problem, i.e, asked to find the value of $x + y$?	Definition 10 TRY to manipulate the given equation (s) so that the COMBO is isolated on one side of the equation. ONLY try to solve for the individual variables once you've exhausted all the other avenues.
Term 11	Definition 11
Term 12 What are the MADS manipulations in relation to solving most COMBO problems?	Definition 12 M Multiply/Divide by the WHOLE equation by a single number A Add/Subtract a number on BOTH SIDES of the equation D Distribute or factor an expression on ONE side of the equation S Square/Unsquare both sides of the equation

<p>Term 13</p> <p>To solve for a variable combo, what should you do?</p>	<p>Definition 13</p> <p>Isolate the combo on one side of the equation</p>
<p>Term 14</p> <p>In DS problems, when you detect that it may involve a combo, you should try to manipulate the equation(s) in either the question or the statement so that the combo is isolated on one side of the equation. Then, how do you tell if the equation is SUFFICIENT? What about NOT SUFFICIENT?</p>	<p>Definition 14</p> <p>Sufficient: The other side of an equation from a statement contains a VALUE.</p> <p>NOT Sufficient: The other side of the equation contains a VARIABLE EXPRESSION</p>
<p>Term 15</p>	<p>Definition 15</p>

Term 16 What are the 3 steps for solving ABSOLUTE VALUE EQUATIONS?	Definition 16 1. ISOLATE the Absolute Value expression 2. Once you have an equation of the form $x = a$ and $a > 0$, you know that $x = (+ -) a$... Remove the absolute value brackets and solve the RHS of the equation for 2 DIFFERENT CASES.
Term 17 Once we have an equation of the form $x = a$, and $x > 0$, what do we know about x ?	Definition 17 $x = (+-) a$
Term 18 What rule is essential to follow when solving ABSOLUTE VALUE EQUATIONS?	Definition 18 To make sure to solve for BOTH cases.

Term 19 Why are EVEN EXPONENTS dangerous?	Definition 19 Because they hide the sign of the base, and can have a POSITIVE and a NEGATIVE solution!
Term 20 $x^2 = 25$ $ x = 5$ What do these have in common? What rule to explain this?	Definition 20 In both cases, $x = (+ -)5$ RULE: for any x, $\text{sqrt.}(x) = x$
Term 21 Solve: $x^2 + 9 = 0$	Definition 21 $x^2 = -9$ Therefore x has NO SOLUTION (squaring can NEVER product a negative number!)

Term 22 How many solutions does an equation with an odd exponent have?	Definition 22 1 only
Term 23 How would you solve problems that involve exponential expressions on BOTH sides of the equation ?	Definition 23 REWRITE the bases so that either the same base, or the same exponent, appears on both sides of the exponential equation. THEN you can usually eliminate the bases or the exponents, writing what's left over as an equation...
Term 24 $0^x = 0^y$ so, $x=y$... True or false? Why?	Definition 24 FALSE Because for example $0^2=0^5=0^{11}$ etc. So, we can't claim that $x = y$

Term 25

$$1^a = 1^d$$

so, $a=d$...

True or false? Why?

Definition 25

FALSE

Because for example

$$1^2 = 1^5 = 1^{11} \text{ etc.}$$

So, we can't claim that $a = d$

Term 26

When are you allowed to divide by a variable, (or ANY expression) ?

Definition 26

When you are absolutely sure the variable or expression $\neq 0$

Term 27

Be careful not to assume that a quadratic equation always has _____. Always _____ quadratic equations to determine their solutions. This will enable you to see whether a quadratic equation has _____ or _____ solutions.

Definition 27

Be careful not to assume that a quadratic equation always has **TWO SOLUTIONS**. Always **FACTOR** quadratic equations to determine their solutions. This will enable you to see whether a quadratic equation has **ONE** or **MORE** solutions.

Term 28

$$x^2 - y^2 = ?$$

Definition 28

$$(x + y)(x - y)$$

Term 29

$$x^2 + 2xy + y^2 = ?$$

Definition 29

$$(x + y)(x + y) = (x + y)^2$$

Term 30

$$x^2 - 2xy + y^2 = ?$$

Definition 30

$$(x - y)(x - y) = (x - y)^2$$

Term 31 $a^2 - 1 = ?$	Definition 31 $(a - 1)(a + 1)$
Term 32 $(a + b)^2 = ?$	Definition 32 $a^2 + 2ab + b^2$
Term 33 Solve: $a^2 + b^2 = 9 + 2ab$	 Step 1. $a^2 + b^2 - 2ab = 9$ Step 2. $(a - b)^2 = 9$ Step 3. $a - b = (+ -)$ 3 ... (important step!)

Term 34

$$(x + y)^2 = x^2 + y^2 ?$$

TRUE or FALSE?

Definition 34

FALSE

$$(x + y)^2 = x^2 + 2xy + y^2$$

Term 35

$$(x - y)^2 = x^2 - y^2 ?$$

TRUE/FALSE?

Definition 35

FALSE

$$(x - y)^2 = x^2 - 2xy + y^2$$

Term 36

Always try to ____ a quadratic
equation before solving

Definition 36

Always try to **FACTOR** a
quadratic equation before
solving

Term 37	Definition 37
Term 38 At first glance, is the following solveable? Why/Why not? $70A + 5B = 63$	Definition 38 No - because there are 2 variables and only one equation.
Term 39	Definition 39